Specifying Binding and Commitment with Ghost Outputs and Strong Refinement

Hagit Attiya, Technion

With: Constantin Enea, Jennifer Welch and Itay Flam

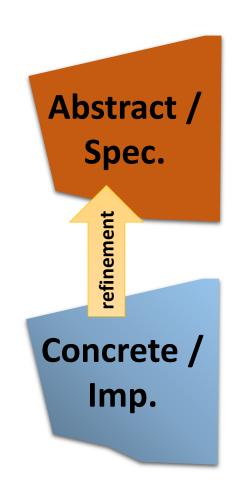
Abstraction for Distributed Protocols

Abstraction and refinement are successful tools for specifying and verifying concurrent data structures

Less so for distributed protocols, which are often specified by listing their properties

Part of the problem is inadequate specification tools

Suggest a path for (partially) dealing with it



Case in Point: Crusader Agreement

Agreement A

[Dolev, 1982]

- (A1) All the reliable processors that do not explicitly know that z is faulty agree on the same message.
 - (A2) If z is reliable, then all the reliable processors agree on its message.

Agreement B

- (B1) All the reliable processors agree on the same message.
- (B2) If z is reliable, then all the reliable processors agree on its r

Agreement B was named the *Byzantine Generals Problem* by Lampd [3]. Here it is referred to as the *Byzantine Agreement*. For con Agreement A is called the *Crusader Agreement*.

Crusader Agreement, More Precisely

[Abraham, Ben-David, Yandamuri, 2022]

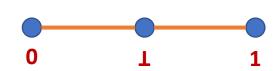
As in standard

Crusader Agreement [15], this functionality is similar to agreement, but allows some parties to output a special \bot value. More specifically, it guarantees (1) Validity: when all non-faulty parties have the same input, this is the only output; and (2) Agreement: no two honest parties output two distinct non- \bot values.

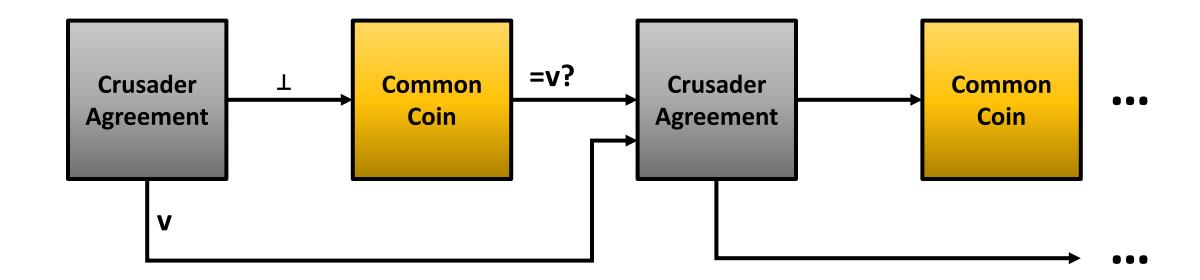
[Attiya, Welch, 2023]

A process starts at one of the end vertexes and decides on a vertex, s.t.

- 1. If all start at the same vertex \Rightarrow decide on this vertex (validity)
- 2. Decided vertexes are adjacent (agreement)

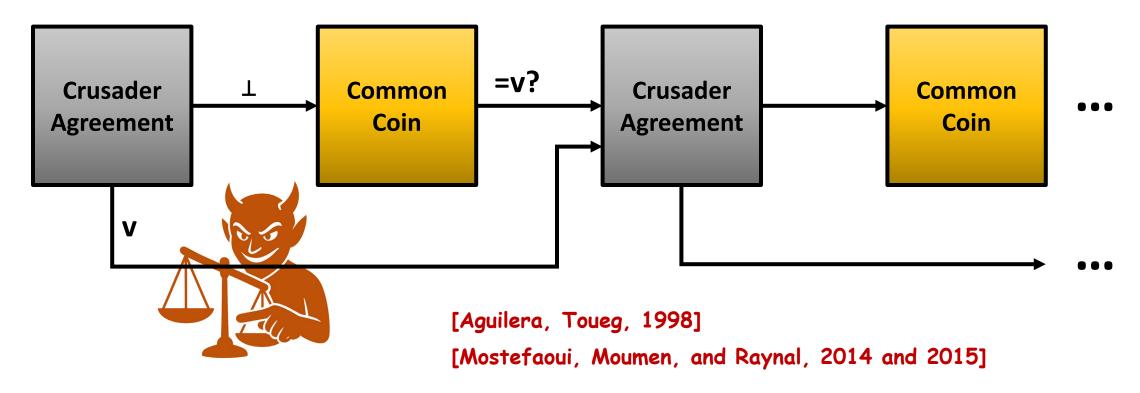


Crusader Agreement in Randomized Consensus (Simplified)



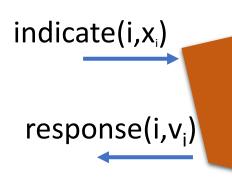
Crusader Agreement in Randomized Consensus: What Could Go Wrong?

Adaptive adversary can exploit the uncertainty to prohibit termination



Crusader Agreement Specification

Use a **ghost** (auxiliary) variable to capture the non- \perp value



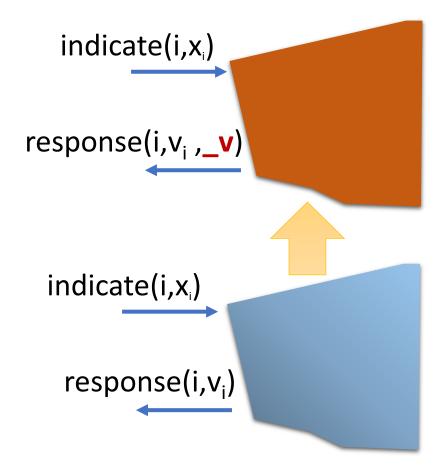
Auxiliary variables (history or prophecy) are typically added to an implementation to prove its correctness

[Abadi, Lamport 1991] [Marcus, Pnueli AMAST 1996]



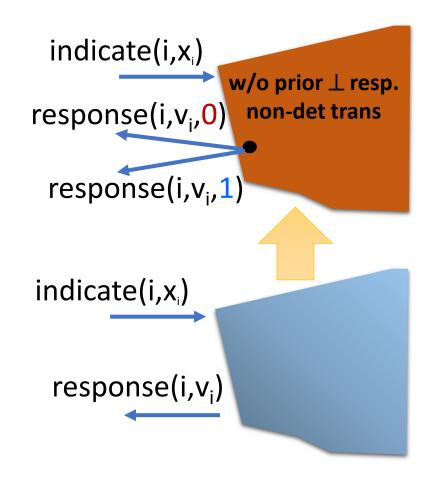
We'll add them to the specification, in part., its interface

- _v is the same in all responses
- _v is the input of some correct process
- If $v_i \leftrightarrow \bot$ then $v_i = _v$

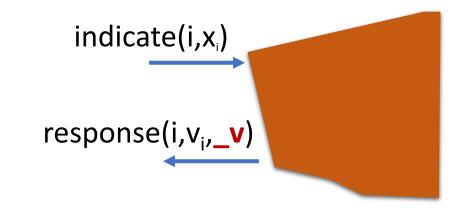


- _v is the same in all responses
- _v is the input of some correct process
- If $v_i \leftrightarrow \bot$ then $v_i = _v$

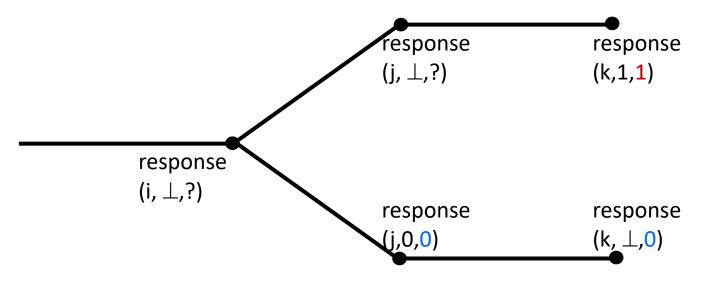
Hides a non-deterministic choice of the ghost output



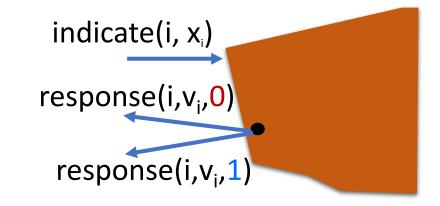
- _v is the same in all responses
- _v is the input of some correct process
- If $v_i \leftrightarrow \bot$ then $v_i = _v$

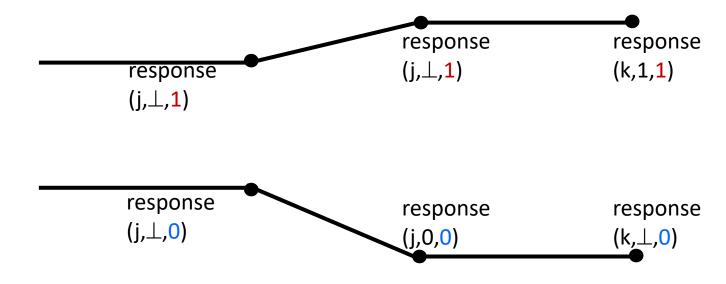






In a CA implementation,
_v might be determined by the future,
i.e., it is a prophecy variable





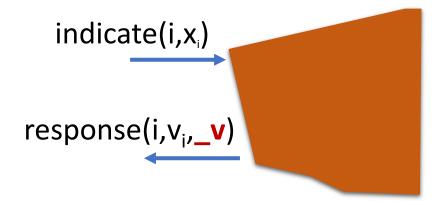
Trace Property

Hagit Attiya FRIDA @ DISC 2025

Binding Crusader Agreement

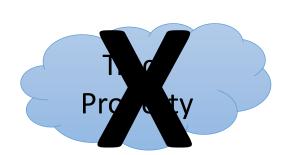
[Abraham, Ben-David, Yandamuri, 2022][Attiya, Welch, 2023]

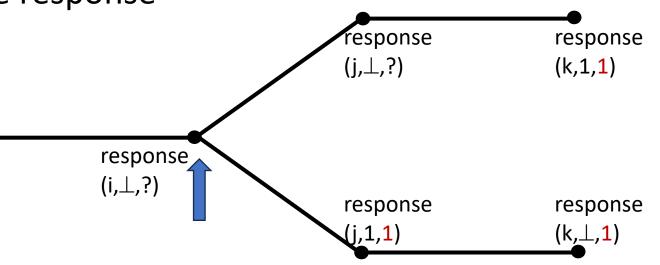
Same non-\preceq value is decided in all extensions after the first correct process returns



Adversary cannot bias the response

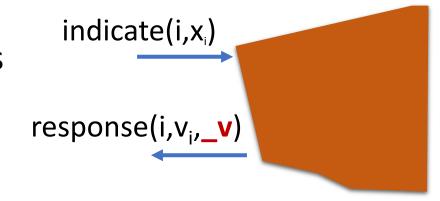
Not a trace property

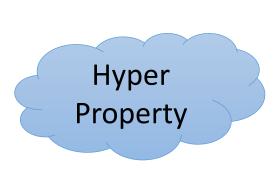


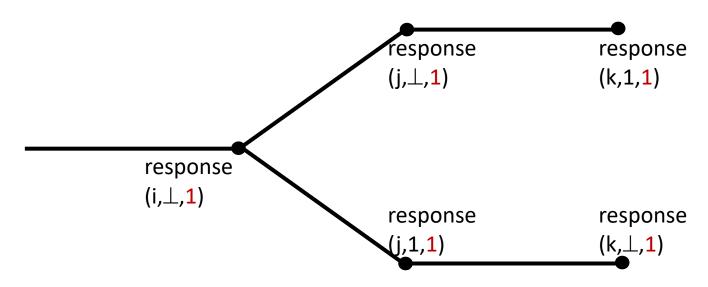


Binding Crusader Agreement

Same non-\(\perp \) value is decided in all extensions after the first correct process returns

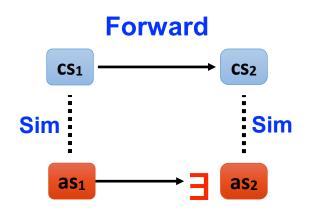


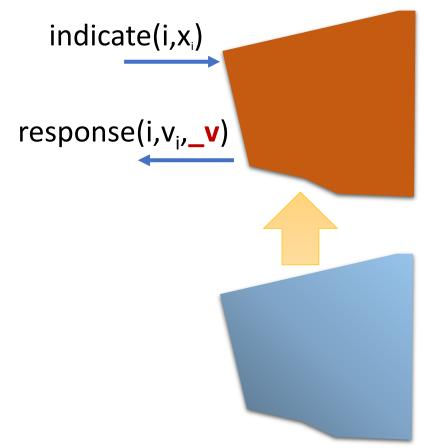




Implementing the CA Specification

Refine the CA specification by relating states of the abstract and concrete objects

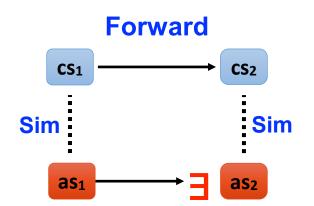


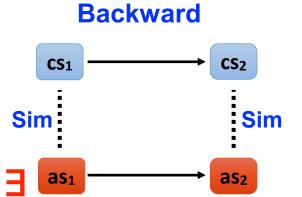


Forward simulations rely only on history leading to the current state

Implementing the CA Specification

Refine the CA specification by relating states of the abstract and concrete objects





Backward simulations are prophecies that determinize the future

Refinement can be proved by forward & backward simulation

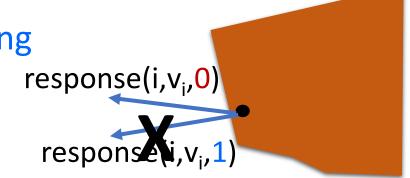
[Lynch, Vaandrager][Jonsson]

indicate(i,x_i)

response(i,v_i,_v)

Binding CA and Strong Refinement

A crusader agreement implementation is binding if it is a strong refinement of the specification r



Obj \leq_s Spec iff \forall program P, \forall deterministic scheduler S_1 of P X Obj, \exists deterministic scheduler S_2 of P X Spec, $\mathsf{Traces}(P\ X\ \mathsf{Obj}\ X\ S_1) = \mathsf{Traces}(P\ X\ \mathsf{Spec}\ X\ S_2)$

≡Forward Simulation from the implementation to the specification

[Attiya, Enea, DISC 2019]

v is a history variable (no non-determinism)

[Attiya, Enea, DISC 2019]

[Attiya, Ene

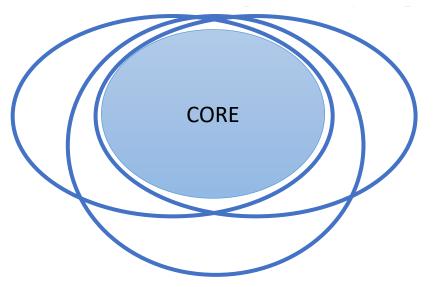
Another Example: Gather

Implicit in [Canetti, Rabin 1993]

[Abraham, Jovanovic, Maller, Meiklejohn, Stern, and Tomescu 2021]

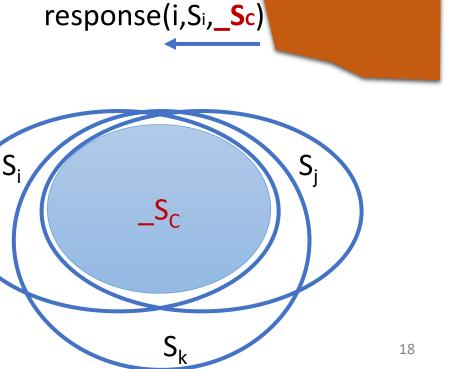
Gather is a natural multi-dealer extension of Reliable Broadcast where every party is also a dealer. The output of a gather protocol is a gather-set. A gather-set consists of at least n-f pairs (j,x), such that $j \in [n], x \in \mathcal{M}$, and each index j appears at most once. For any given gather-set X, we define its index-set $Indices(X) = \{j | \exists (j,x) \in X\}$ to be the set of indices that appear in X.

Intuitively speaking, the goal of Gather is to have some common *core* gather-set such that all parties output a super-set of this core.



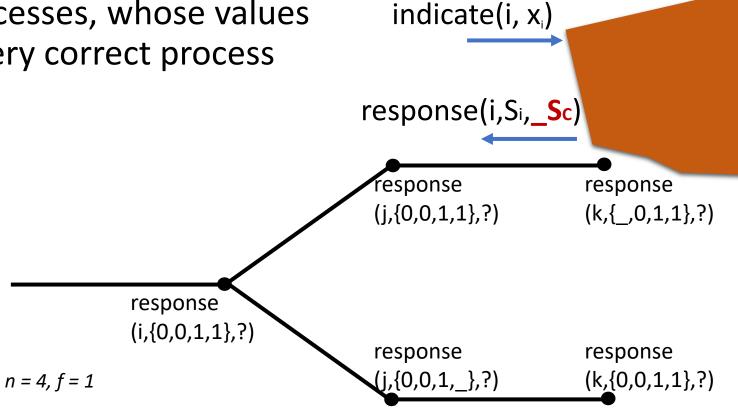
Gather with a Ghost Output

- ✓ For process k, and every pair of nonfaulty processes i and j, if (k,x_i) is in S_i and (k,x_j) is in S_j , then $x_i = x_j$ indicate(i, x_i)
- ✓ For every pair of correct processes i and j, if (j,x) is in S_i , then $x = x_i$
- For every correct process, $S_i \supseteq _S_C$
- $|S_c| \ge n f \Rightarrow |S_i| \ge n f$



Common Core

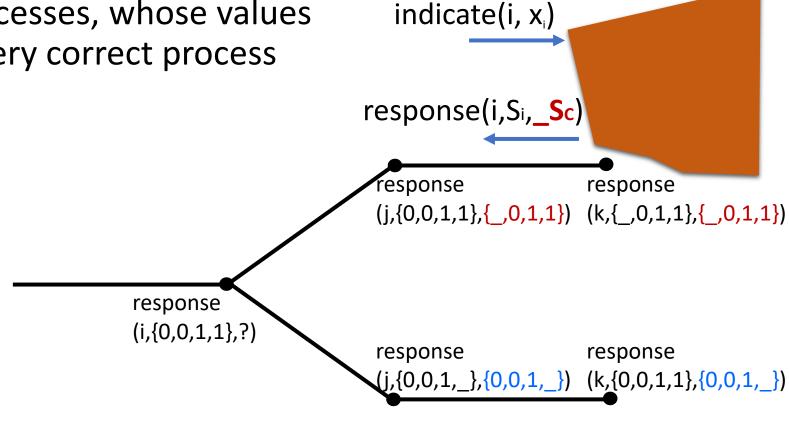
there is a set of n-f processes, whose values appear in the set of every correct process



Trace Property

Common Core

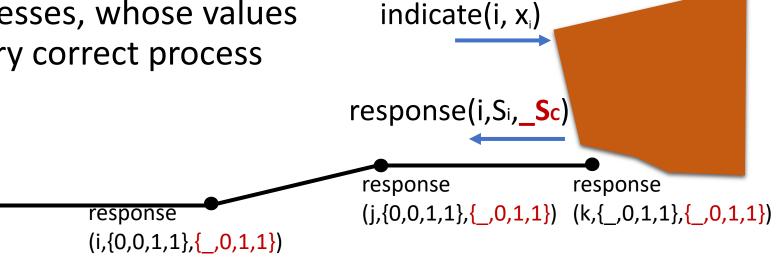
there is a set of n-f processes, whose values appear in the set of every correct process



Trace Property

Common Core

there is a set of n-f processes, whose values appear in the set of every correct process



Trace Property response response $(i,\{0,0,1,1\},\{0,0,1,_\})$ $(j,\{0,0,1,_\},\{0,0,1,_\})$ $(k,\{0,0,1,1\},\{0,0,1,_\})$

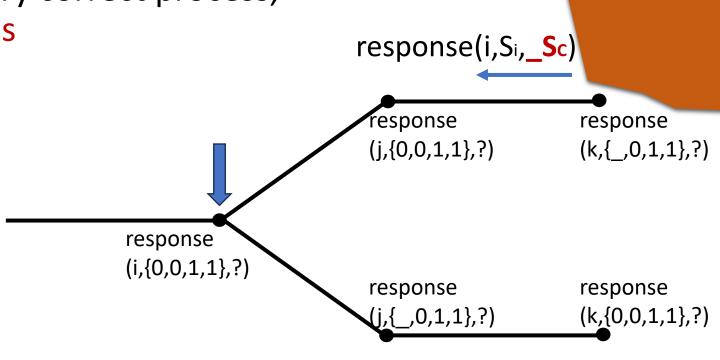
Binding Common Core

When the first correct process returns

there is a set of n-f processes, whose values

appear in the set of every correct process,

in all possible extensions

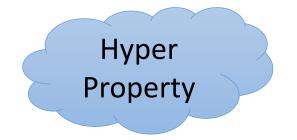


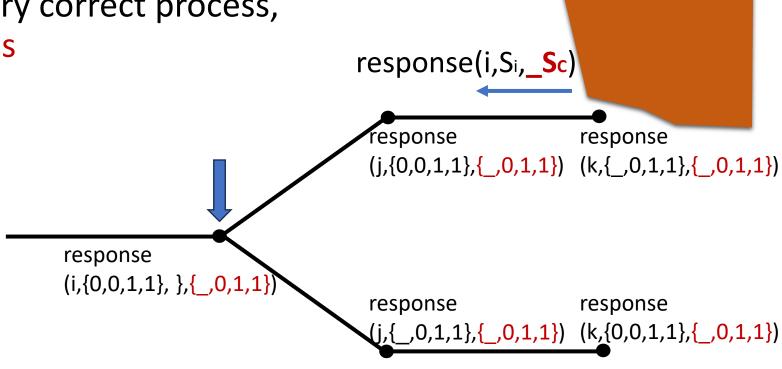
indicate(i, x_i)



Binding Common Core

When the first correct process returns there is a set of n-f processes, whose values appear in the set of every correct process, in all possible extensions





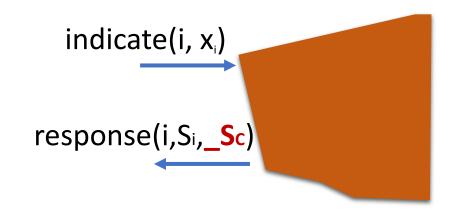
indicate(i, x_i)

Binding Gather and Strong Refinement

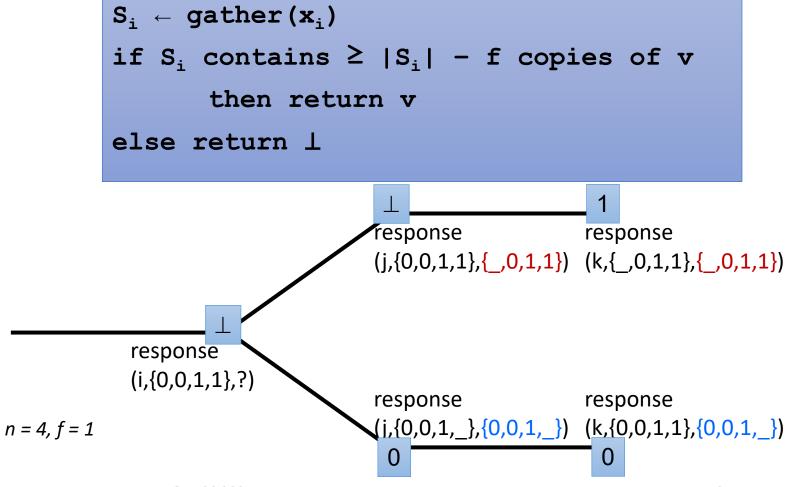
Implementation is binding if it is a strong refinement of the gather module

■Forward Simulation

_Sc is a history variable



Crusader Agreement from Gather (code for p_i)



Crusader Agreement from Gather (key lemma)

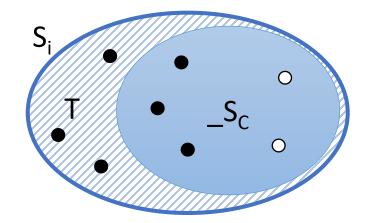
```
S_i \leftarrow gather(x_i)
if S_i contains \geq |S_i| - f copies of v
then return v
else return \perp
```

Lemma: If a non- \bot value \lor is returned by a correct process, then \lor appears $\ge |_S_C|$ -f times in the common core $_S_C$

This suffices since $|S_c| = n - f$ and n > 3f

- ⇒ at most one value appears |_S_C | f times in _S_C
- ⇒ all correct processes that return a non-⊥ value return the same value

Crusader Agreement from Gather (key lemma)



```
S_i \leftarrow gather(x_i)

if S_i contains \geq |S_i| - f copies of v

then return v

else return \bot
```

Lemma: If a non- \bot value \lor is returned by a correct process, then \lor appears $\ge |_S_C|$ -f times in the common core $_S_C$

Proof of the lemma: correct process p_i returns v appearing $|S_i|$ -f times in S_i Let T be $S_i \setminus S_c$. $|T| = |S_i| - |S_c| \le f$

Then the number of times v appears in $_{S_c}$ is the number of times it appears in $_{S_i}$ minus the number of times it appears in $_{T_c}$ which is $\geq |_{S_i}| - f - (|_{S_i}| - |_{S_c}|)$

Crusader Agreement from Gather: Binding

```
S_i \leftarrow gather(x_i)
if S_i contains \geq |S_i| - f copies of v
then return v
else return \perp
```

If _S_C is a history variable (as ensured by strong refinement), then CA is binding response response (j,{0,0,1,1},{_,0,1,1})

Otherwise, _S_c is a prophecy variable, and CA is not binding (recall previous example)

response response (j,{_,0,1,1},{_,0,1,1}) (k,{0,0,1,1},{_,0,1,1})

Hagit Attiya FRIDA @ DISC 2025 28

(i,{0,0,1,1},{_,0,1,1})

response

A Glimpse of What's Next

Commitment is a hyperproperty: a process commits to a value v (often drawn at random), unknown to other processes

In all extensions, only v can be revealed

But what about random secret draw?

Implicitly used for a common coin in [Canetti, Rabin 1993]

[Freitas, Kuznetsov, Tonkikh, DISC 2022]

Process p_i commits to a random value v, unknown to all processes

(Single) Random Secret Draw: Ghost Output

A single process commits to a random value $d \in [1, ..., D]$ indicate_draw(i) response_draw(i,_d)

Also, ensure that d stays secret until revealed (using non-interference)

Wrap-Up

- Binding is a hyperproperty that commits the outputs across all extensions
- Ghost outputs can expose hidden commitments
- Strong refinement (≡ forward simulation, based only on the history) enforces binding
- Composition preserves binding:
 E.g., gather ⇒ crusader agreement
- Future research: commitment of probabilistic distributions

THANKS!